Can you obtain a new Texas death certificate for me then rush apostille or authenticate it?

No, we can't.

You will need to contact the Texas county where the official death occurred and then order a new certified Texas death certificate from that county office.